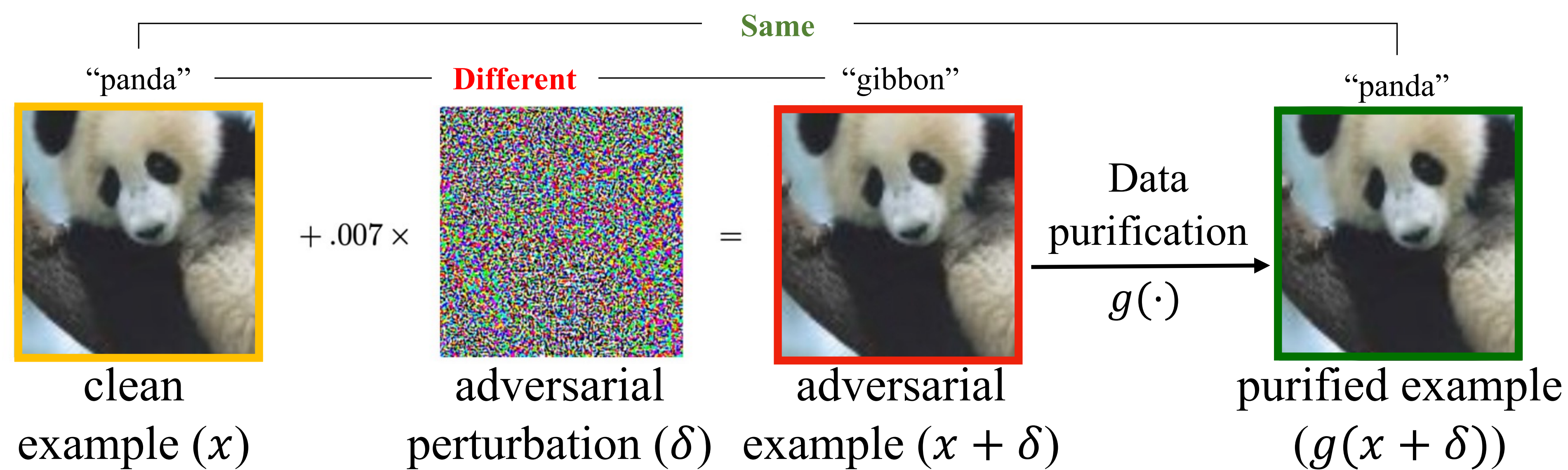




## Background



The figure is modified based on: Explaining and Harnessing Adversarial Examples. ICLR 2015.

**Adversarial Attack:**  $f(x') = y' \neq f(x) = y$ ,  
where  $x' = x + \delta$ ,  $\delta = \arg \max_{\delta \leq \epsilon} \mathcal{L}(f(x + \delta), y)$

**Adversarial Training (AT):**  $f'(x') = y$ ,  
where robust model  $f'$  is trained with adversarial examples  $x'$  and true label  $y$ .

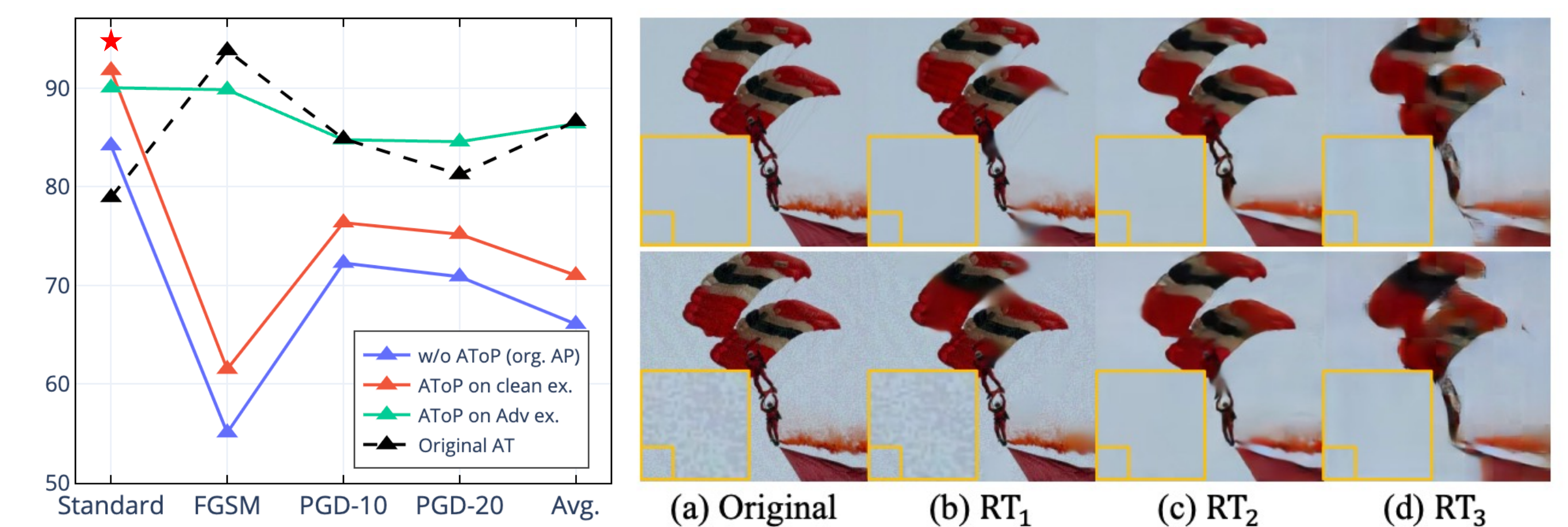
**Adversarial Purification (AP):**  $f(g(x')) = y$ ,  
\*where purifier model  $g$  is a pre-trained generator.

## Experimental results

Table 6: Standard accuracy and robust accuracy against AutoAttack  $l_\infty$  ( $\epsilon = 8/255$ ),  $l_2$  ( $\epsilon = 1$ ) and StAdv non- $l_p$  ( $\epsilon = 0.05$ ) threat models on CIFAR-10 with ResNet-50 classifier model.

Defense method	Standard Acc.	$l_\infty$	$l_2$	StAdv
Standard Training	94.8	0.0	0.0	0.0
Adv. Training with $l_\infty$ (Laidlaw et al., 2021)	86.8	49.0	19.2	4.8
Adv. Training with $l_2$ (Laidlaw et al., 2021)	85.0	39.5	47.8	7.8
Adv. Training with StAdv (Laidlaw et al., 2021)	86.2	0.1	0.2	53.9
Adv. Training with all (Laidlaw et al., 2021)	84.0	25.7	30.5	40.0
PAT-self (Laidlaw et al., 2021)	82.4	30.2	34.9	46.4
Adv. CRAIG (Dolatbadi et al., 2022)	83.2	40.0	33.9	49.6
DiffPure (Nie et al., 2022)	88.2	70.0	70.9	55.0
Ours	<b>89.1</b>	<b>71.2</b>	<b>73.4</b>	<b>56.4</b>

Figure 4a: Comparison of AT, AP and AToP. Figure 3: Clean (Top) and adversarial examples (Bottom).



### Adversarial Training on Purification (AToP)

- [✓] Achieve optimal robustness on known attacks.
- [✓] Keep generalization against unseen attacks.
- [✓] Achieve optimal accuracy on clean examples.

Table 7: Standard accuracy and robust accuracy of attacking the classifier model on CIFAR-10 with ResNet-18. All attacks are  $l_\infty$  threat model with  $\epsilon = 8/255$ .

Transforms	AToP	Standard Acc.	FGSM	PGD-10	PGD-20	PGD-1000
RT <sub>1</sub>	×	<b>93.36</b>	16.60	0.00	0.00	0.00
	✓	<b>93.36</b>	<b>91.99</b>	<b>43.55</b>	<b>36.72</b>	<b>39.45</b>
RT <sub>2</sub>	×	84.18	55.08	72.27	70.90	67.97
	✓	<b>90.04</b>	<b>89.84</b>	<b>84.77</b>	<b>84.57</b>	<b>84.38</b>
RT <sub>3</sub>	×	75.98	67.97	70.51	70.70	70.31
	✓	<b>80.02</b>	<b>70.90</b>	<b>73.05</b>	<b>72.07</b>	<b>73.44</b>

More complex RT can better remove perturbations, but also result in a loss of semantic information. Accuracy ↑  
Accuracy ↓

**Conclusion:** We develop a novel efficient defense technology by combining AT and AP, which can **learn a robust purifier**.

**Limitations:** AToP requires training on the purifier, and as the complexity of purifier increases, so does the training cost.

## Related works

Table 1: Robustness comparison of defenses with expectation (negative impacts are marked in red).

Defense method	Clean images	Known attacks	Unseen attacks
Vanilla model	~94%	~0%	~0%
Expectation	=	↑↑	↑
AT	↓↓	↑↑	N/A
AP	↓	↑	↑
AToP (ours)	≈	↑↑	↑

### Adversarial Training (AT)

- [✓] Achieve optimal robustness on known attacks.
- [X] Vulnerable to unseen attacks.
- [X] Reduce the accuracy of clean examples.

### Adversarial Purification (AP)

- [✓] Keep generalization against unseen attacks.
- [X] Weaker robustness than AT on known attacks.
- [X] Slightly reduce the accuracy of clean examples.

The pre-trained purifier model is not good enough for classification and non-robust itself.

## Method

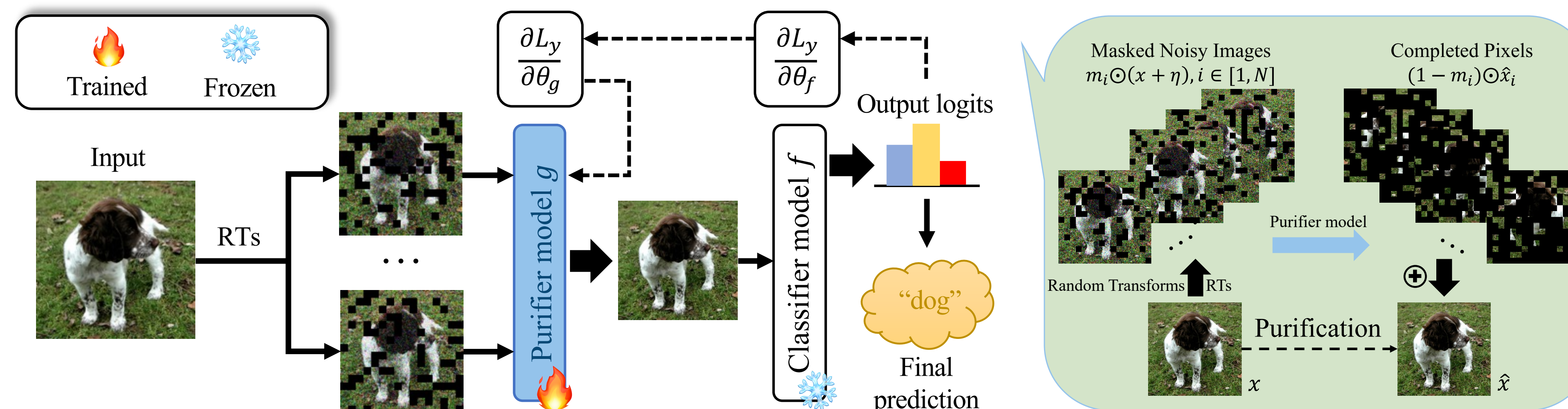


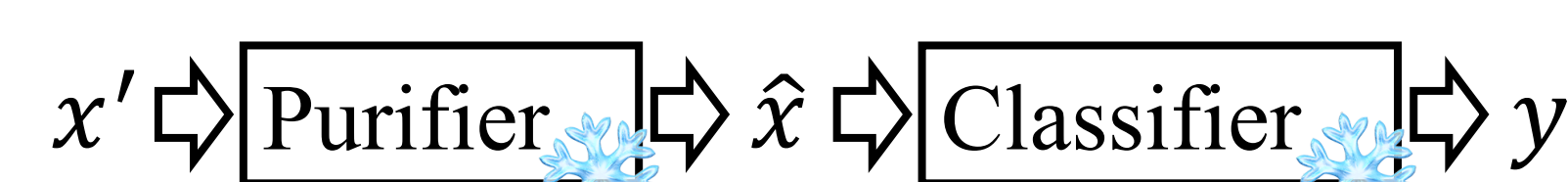
Figure 1: Illustration of adversarial training on purification (AToP). To fine-tune the purifier with adversarial training, we aim to optimize the model by freezing classifier parameters and only updating purifier parameters.

AT: **Learning** a robust **classifier model**.



Based on the **pre-trained generator model** trained by the original generative loss  $\ell_g$ :  
 $L_{\theta_g} = \ell_g(x, \theta_g)$ .

AP\*: **Utilizing** a pre-trained generator as **purifier**.



We incorporate a classification loss  $\ell_{cls}$  to **fine-tune the generator model** with  
a) clean examples  $x$  and labels  $y$ :

$$L_{\theta_g} = \ell_g(x, \theta_g) + \lambda \cdot \ell_{cls}(x, y, \theta_g, \theta_f)$$

b) adversarial examples  $x'$  and labels  $y$ :

$$L_{\theta_g} = \ell_g(x', \theta_g) + \lambda \cdot \ell_{cls}(x', y, \theta_g, \theta_f)$$

AToP: **Learning** a robust **purifier model**.